



## Mathematics and CS Seminar

# GeomTop seminar: Non-Topological Persistence for Computer Vision

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**Host: Herbert Edelsbrunner**

Persistent Homology (PH) provides a mathematical description of a data set that captures its internal structure (relations) at multiple scales in a robust manner [3]. These properties made of PH a widely used tool in applications [4]. However, PH requires the dataset to be represented as a topological space, usually as a simplicial complex whose homology group can be computed via efficient algorithms. In this talk, we will build on the non-topological persistence framework introduced in [1,2], which allows us to define persistence diagrams (PDs) in other categories than FinSimp (e.g., weighted graphs, quivers, metric spaces) and arbitrary functors (e.g., edge-block and clique communities). We will discuss two general ways for producing persistence functions, and some examples coming from graph theory and image processing. We will introduce a non-topological persistence construction that allows for the detection of the boundary of objects in images, and that is robust to noise, e.g. salt and pepper, and Gaussian noise. We will use this construction, that we named persistence pooling, to define a new pooling layer for Convolutional Neural Networks. The persistence pooling layer associates a PD to each patch. The pixels will be consequently sorted in a list following their lifetime. The final output will be obtained averaging this list with a list of learnable weights. Preliminary results will be presented showing the performances of this layer on the Fashion-MNIST dataset [5].

[1] Bergomi, M.G., Ferri, M., Vertechi, P., Zuffi, L. (2019), Beyond topological persistence: Starting from networks, arXiv.

[2] Bergomi, M.G., Vertechi, P. (2019), Rank-based persistence, arXiv.

[3] Cohen-Steiner, D., Edelsbrunner, H., & Harer, J. (2007). Stability of persistence diagrams. *Discrete & Computational Geometry*, 37(1), 103-120.

**Wednesday, November 20, 2019 04:30pm - 05:30pm**

IST Austria Campus Mondri Seminar Room 3, Central Building



(2017). Persistent topology for natural data analysis: A survey. In *Towards Integrative Mining and Knowledge Extraction* (pp. 117-133). Springer, Cham.  
This invitation is valid as a ticket for the IST Shuttle from and to Heiligenstadt Station. Please find a schedule of the IST Shuttle on our webpage: <https://ist.ac.at/en/campus/how-to-get-here/>. The IST Shuttle bus is marked IST Shuttle (#142) and has the Institute Logo printed on the side.

[5] Rasul, K., Vollgraf R. (2017), Fashion-MNIST: a Novel Image Dataset for Benchmarking Machine Learning Algorithms, arXiv